

Supplementary Results

Galvin et al. (2003) emphasized that assuming a normal distribution in Type II tasks is unreasonable. In addition, Type II d' is influenced by the performance of Type I tasks. Thus, we calculated meta-d' and meta-d'/d' according to Maniscalco and Lau (2012, 2014). Meta-d' is a measure of metacognitive sensitivity unaffected by the performance of Type I tasks. Meta-d'/d' reflects metacognitive efficiency. Meta-d'/d' = 1 signifies using all information from Type I tasks in Type II tasks; meta-d'/d' < 1 indicates a lack of information; meta-d'/d' > 1 refers to using additional information (Maniscalco & Lau ,2012).

We used both *trials2counts.m* and *fit_meta_d_MLE.m* codes to estimate meta-d' (Maniscalco & Lau, 2012, 2014). Data from three participants were excluded from the uniform and one from the Zipfian distribution conditions because of the following error. The message was not produced in the low-frequency Zipfian distribution condition when estimating meta-d'.

Error using barrier Objective function is undefined at initial point. fmincon cannot continue.

Similar to the results of Type II d', a significant difference was detected in meta-d' between the uniform and Zipfian distribution conditions, t(62) = 2.18, p = .033, $BF_{10} = 1.86$, d = 0.54, 95% CI [0.05, 1.14]. This difference indicated that meta-d' in the Zipfian distribution (mean = 1.73, SE = 0.21) was significantly larger than in the uniform distribution condition (mean = 1.13, SE = 0.17). However, meta-d' in the low-frequency Zipfian distribution (mean = 1.40, SE = 0.21) was similar to the uniform distribution condition t(63) = .976, p = .333, $BF_{10} = 0.38$, d = 0.24, 95% CI [-0.28, 0.81]. Furthermore, meta-d'/d' was significantly higher than 1 in the Zipfian distribution condition, mean = 1.07 (SE = 0.14), t(32) = 3.47, p = .002, $BF_{10} = 0.21$, d = 0.59, 95% CI [1.30, 2.15]. This value was marginally lower than 1 in the low-frequency Zipfian distribution condition, mean = 0.97 (SE = 0.16), t(33) = 1.91, p = .065, $BF_{10} = 0.19$, d = 0.32, 95% CI [0.97, 1.82]. However, meta-d'/d' in the uniform distribution condition was not significantly different from 1, mean = 0.97 (SE = 0.33), V = 295.00, p = .367, $BF_{10} = 0.19$, r = 0.16, 95% CI [0.78, 1.48]. Note that Bayes factor values in one-sample tests were under 1 in all conditions. These results suggest that Zipfian distributions enhance metacognitive sensitivity to familiarity decisions. Moreover, all information was utilized in the post-decision wagering task across distribution conditions.

References

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¹ We conducted a Wilcoxon signed-rank test because a Shapiro-Wilk test showed a deviation from normality (W = .841, p < .001).

Supplementary Table 1Line drawings arranged into each triplet in the uniform distribution condition

| participants | Α | В | С | D | Е | F | G | Н | <u>l</u> | J | K | L | М | N | 0 | Р | Q | R |
|--------------|-----------|-----------|-----------|-----------|-----------|-----------|----------|-----------|-----------|----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| 1 | cat | key | butterfly | chair | ball | fish | bottle | watch | fork | car | flower | book | dog | shoe | airplane | cake | house | banana |
| 2 | flower | dog | cake | fish | ball | car | cat | watch | key | shoe | chair | airplane | banana | house | bottle | fork | butterfly | book |
| 3 | cake | key | bottle | cat | house | fish | car | fork | flower | airplane | shoe | ball | chair | book | butterfly | banana | watch | dog |
| 4 | fork | book | fish | dog | house | airplane | bottle | key | chair | watch | cake | flower | car | ball | banana | butterfly | cat | shoe |
| 5 | fork | cat | butterfly | airplane | book | flower | fish | ball | chair | banana | key | watch | house | dog | cake | shoe | bottle | car |
| 6 | flower | butterfly | cake | shoe | fork | car | chair | dog | ball | house | bottle | banana | airplane | cat | book | key | fish | watch |
| 7 | key | airplane | butterfly | book | cat | bottle | fish | car | chair | flower | ball | banana | house | watch | cake | dog | fork | shoe |
| 8 | key | book | cake | fork | airplane | dog | bottle | shoe | butterfly | banana | watch | house | flower | ball | chair | car | fish | cat |
| 9 | banana | fish | watch | dog | chair | butterfly | shoe | airplane | house | ball | car | book | cat | cake | bottle | key | fork | flower |
| 10 | shoe | house | chair | cat | fish | flower | banana | cake | watch | ball | butterfly | fork | book | key | bottle | dog | airplane | car |
| 11 | ball | book | shoe | cat | dog | butterfly | car | chair | airplane | banana | bottle | fork | watch | key | flower | cake | fish | house |
| 12 | fork | chair | banana | watch | book | key | airplane | bottle | car | house | dog | ball | shoe | cat | fish | flower | butterfly | cake |
| 13 | house | fish | ball | butterfly | fork | shoe | cake | chair | watch | cat | car | book | airplane | key | banana | flower | dog | bottle |
| 14 | ball | book | fish | chair | house | fork | bottle | key | cat | airplane | shoe | watch | flower | car | butterfly | dog | cake | banana |
| 15 | fish | cat | house | car | fork | dog | cake | airplane | bottle | ball | shoe | butterfly | watch | banana | book | flower | chair | key |
| 16 | butterfly | watch | fork | chair | airplane | dog | cat | bottle | house | fish | ball | car | cake | key | book | flower | shoe | banana |
| 17 | flower | cat | cake | fork | chair | fish | car | shoe | ball | dog | watch | bottle | banana | book | airplane | butterfly | key | house |
| 18 | key | shoe | ball | watch | butterfly | fork | airplane | cat | flower | dog | cake | chair | book | house | bottle | banana | fish | car |
| 19 | house | dog | cake | fork | cat | chair | ball | flower | shoe | watch | book | fish | butterfly | bottle | car | banana | key | airplane |
| 20 | shoe | flower | fork | bottle | watch | banana | cake | butterfly | car | cat | dog | house | fish | book | ball | airplane | chair | key |
| 21 | shoe | banana | bottle | dog | fish | cake | fork | cat | house | flower | butterfly | chair | airplane | key | car | ball | watch | book |
| 22 | cat | butterfly | flower | house | cake | chair | fork | car | fish | dog | bottle | key | airplane | ball | banana | shoe | book | watch |
| 23 | cat | watch | ball | cake | butterfly | house | bottle | key | fish | banana | chair | airplane | flower | book | car | dog | fork | shoe |
| 24 | key | dog | cat | cake | fork | bottle | chair | banana | house | book | watch | flower | ball | shoe | airplane | butterfly | car | fish |
| 25 | book | cake | fish | car | flower | airplane | house | shoe | watch | bottle | butterfly | dog | ball | key | fork | chair | banana | cat |
| 26 | house | dog | ball | cat | key | chair | fork | shoe | car | flower | bottle | fish | banana | butterfly | book | airplane | cake | watch |
| 27 | ball | watch | fork | book | car | fish | banana | dog | cat | flower | airplane | butterfly | bottle | cake | key | house | shoe | chair |
| 28 | banana | shoe | car | book | cat | fork | airplane | chair | house | cake | dog | butterfly | watch | flower | key | bottle | fish | ball |
| 29 | house | ball | book | flower | dog | car | bottle | shoe | cat | fork | banana | fish | watch | airplane | cake | key | chair | butterfly |
| 30 | ball | fish | house | fork | chair | banana | airplane | cat | bottle | book | key | cake | watch | flower | shoe | dog | car | butterfly |
| 31 | fork | book | cat | bottle | car | butterfly | banana | watch | key | house | chair | flower | ball | airplane | cake | dog | shoe | fish |
| 32 | cat | fork | butterfly | car | house | key | ball | dog | airplane | fish | flower | watch | shoe | banana | chair | cake | bottle | book |
| 33 | cake | fork | key | house | fish | banana | bottle | book | shoe | car | dog | watch | cat | butterfly | ball | chair | flower | airplane |
| 34 | book | fish | butterfly | cake | banana | cat | ball | car | bottle | chair | fork | house | watch | airplane | shoe | flower | dog | key |
| 35 | cat | chair | house | airplane | banana | watch | book | flower | shoe | fork | ball | car | cake | dog | fish | key | bottle | butterfly |

Supplementary Table 2 *Line drawings arranged into each triplet in the Zipfian distribution condition*

| participants | Α | В | С | D | Е | F | G | Н | I | J | К | L | М | N | 0 | Р | Q | R |
|--------------|-----------|-----------|-----------|-----------|----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| 1 | house | bottle | cake | shoe | fork | flower | fish | car | dog | watch | butterfly | airplane | book | ball | chair | cat | banana | key |
| 2 | butterfly | fish | flower | banana | key | shoe | dog | house | watch | cat | car | chair | fork | book | ball | airplane | bottle | cake |
| 3 | shoe | airplane | bottle | book | banana | dog | cat | chair | flower | ball | car | house | key | butterfly | cake | fish | fork | watch |
| 4 | fish | ball | dog | airplane | house | cake | butterfly | car | cat | book | key | flower | fork | shoe | bottle | banana | chair | watch |
| 5 | airplane | butterfly | flower | car | banana | cake | chair | key | fork | watch | book | dog | ball | house | fish | cat | shoe | bottle |
| 6 | dog | bottle | watch | airplane | flower | car | ball | fish | house | banana | butterfly | chair | cat | fork | book | key | shoe | cake |
| 7 | ball | fork | butterfly | fish | bottle | key | airplane | cat | book | watch | shoe | banana | dog | flower | house | car | cake | chair |
| 8 | banana | ball | bottle | cat | house | airplane | car | fish | shoe | flower | chair | butterfly | fork | key | book | watch | dog | cake |
| 9 | watch | butterfly | banana | cake | dog | car | bottle | airplane | house | flower | fork | shoe | ball | chair | fish | key | cat | book |
| 10 | banana | cat | cake | book | fork | key | bottle | watch | car | fish | chair | ball | butterfly | flower | shoe | house | airplane | dog |
| 11 | butterfly | fork | ball | dog | house | airplane | chair | cake | watch | flower | key | cat | book | banana | bottle | fish | shoe | car |
| 12 | dog | cake | watch | shoe | cat | chair | bottle | house | fork | butterfly | flower | book | car | ball | banana | key | fish | airplane |
| 13 | chair | fork | airplane | ball | cake | cat | banana | flower | bottle | car | watch | key | shoe | fish | butterfly | book | house | dog |
| 14 | fork | cake | ball | banana | bottle | book | airplane | flower | butterfly | dog | chair | house | fish | cat | key | car | watch | shoe |
| 15 | shoe | fork | flower | banana | bottle | chair | car | butterfly | book | house | dog | fish | cake | airplane | cat | watch | key | ball |
| 16 | book | cat | bottle | butterfly | chair | cake | fish | key | car | banana | dog | ball | fork | flower | shoe | house | airplane | watch |
| 17 | shoe | house | banana | key | fork | fish | airplane | dog | watch | cat | cake | ball | book | bottle | chair | flower | butterfly | car |
| 18 | watch | banana | ball | chair | car | airplane | flower | fish | fork | cake | shoe | house | key | cat | book | bottle | dog | butterfly |
| 19 | banana | cat | fork | butterfly | shoe | bottle | chair | cake | ball | house | car | dog | watch | flower | key | fish | book | airplane |
| 20 | flower | airplane | house | butterfly | fish | dog | ball | chair | shoe | fork | watch | book | cake | car | cat | bottle | banana | key |
| 21 | bottle | house | flower | watch | cat | key | fish | ball | dog | book | airplane | chair | car | banana | butterfly | cake | fork | shoe |
| 22 | flower | butterfly | cat | fork | cake | shoe | house | airplane | dog | bottle | ball | book | banana | key | chair | fish | watch | car |
| 23 | book | shoe | watch | airplane | house | dog | bottle | fork | key | chair | cake | car | flower | butterfly | banana | fish | ball | cat |
| 24 | watch | shoe | fish | butterfly | flower | book | chair | airplane | car | house | cake | fork | dog | cat | ball | bottle | banana | key |
| 25 | shoe | dog | flower | airplane | house | fork | banana | car | bottle | key | cat | book | butterfly | chair | cake | ball | watch | fish |
| 26 | fish | dog | key | fork | airplane | butterfly | watch | house | ball | car | flower | chair | cake | bottle | banana | book | cat | shoe |
| 27 | shoe | fork | airplane | banana | flower | watch | key | book | ball | cat | dog | house | cake | butterfly | car | fish | chair | bottle |
| 28 | watch | fish | fork | car | chair | shoe | house | cat | banana | cake | flower | dog | airplane | bottle | ball | book | key | butterfly |
| 29 | watch | chair | house | fish | bottle | dog | ball | butterfly | key | banana | shoe | book | fork | car | cake | flower | airplane | cat |
| 30 | car | cat | cake | key | banana | ball | watch | book | house | butterfly | dog | chair | bottle | fork | flower | airplane | shoe | fish |
| 31 | butterfly | fork | ball | cat | key | chair | book | fish | car | dog | watch | flower | airplane | cake | bottle | banana | shoe | house |
| 32 | key | airplane | fish | house | car | cat | book | ball | banana | dog | fork | bottle | cake | shoe | watch | chair | flower | butterfly |
| 33 | key | airplane | chair | shoe | flower | house | book | cake | ball | bottle | fork | fish | car | watch | banana | butterfly | cat | dog |
| 34 | chair | car | flower | banana | fork | cake | shoe | book | house | fish | key | butterfly | ball | airplane | cat | bottle | watch | dog |
| 35 | house | cat | fish | cake | chair | key | watch | book | car | airplane | butterfly | ball | bottle | banana | flower | fork | dog | shoe |
| 36 | watch | car | chair | fork | shoe | dog | banana | butterfly | cake | airplane | fish | flower | house | cat | book | ball | bottle | key |
| 37 | shoe | car | airplane | dog | fork | house | fish | flower | cat | chair | cake | banana | bottle | key | watch | butterfly | ball | book |
| 38 | banana | flower | car | airplane | dog | ball | chair | watch | shoe | key | butterfly | cake | house | book | bottle | fork | cat | fish |
| 39 | house | banana | cake | butterfly | cat | flower | dog | ball | key | airplane | fork | bottle | car | watch | chair | book | shoe | fish |