

Supplemental Materials

Ranges of the Estimated Parameters

In the following Tables S1 to S7 we provide the ranges of the estimated parameters for all models in Studies 1 and 2. For the logit model we estimated the n weights w_i for each attribute i , allowed to vary between 0 and ∞ . The parameters used to estimate the probit model were the $n - 1$ weights w_i for $n - 1$ attributes, which were restricted to sum to 1, and the variance v of the normal distributed error component ϵ in the diagonal of the variance–covariance matrix, allowed to vary between 0 and 1,000. Finally, for the MDFT we estimated the $n - 1$ weights w_i allocated to the $n - 1$ attributes, restricted to sum to 1, the variance v of the normal distributed error component ϵ , restricted to values between 0 and 1,000, the sensitivity parameter ϕ_1 , restricted to vary between 0.01 and 1,000, and the decay parameter ϕ_2 , restricted to values between 0 and 1. In Study 1, we fixed the weight parameter w_d , which weights distances in the dominance direction relative to distances in the indifference direction, to a value of 12, following Hotelling et al. (2010) and we estimated its value in Study 2, restricting values to between 1 and 50.

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Table S1

Study 1—Logit Model: Estimated Parameter Ranges of the Attribute Weights (w_1 - w_5)

Quantile	w_1	w_2	w_3	w_4	w_5
Q _{0.25}	1.31	0.55	1.46	0.24	0.59
Q _{0.50}	2.14	1.09	2.86	1.01	0.92
Q _{0.75}	3.61	1.70	4.84	3.01	1.64

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Table S2

Study 1—Probit Model: Estimated Parameter Ranges of the Attribute Weights (w_1 - w_5) and Variance (v)

Quantile	w_1	w_2	w_3	w_4	w_5	v
Q _{0.25}	0.15	0.05	0.20	0.01	0.06	0.02
Q _{0.50}	0.24	0.13	0.30	0.10	0.09	0.02
Q _{0.75}	0.41	0.19	0.45	0.29	0.14	0.03

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Table S3

Study I—MDFT: Estimated Parameter Ranges of the Attribute Weights (w_1 - w_5), Variance (v), Decay Parameter (ϕ_2), and Sensitivity Parameter (ϕ_1)

Quantile	w_1	w_2	w_3	w_4	w_5	v	ϕ_2	ϕ_1
Q _{0.25}	0.10	0.03	0.19	0.05	0.07	0.27	0.02	0.14
Q _{0.50}	0.19	0.10	0.33	0.09	0.10	0.88	0.09	0.42
Q _{0.75}	0.40	0.21	0.50	0.23	0.18	1.64	0.22	1.68

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Table S4

Study 2—Logit Model: Estimated Parameter Ranges of the Attribute Weights (w_1 - w_2)

Quantile	Digital camera		Color printer		Notebook computer		Racing bike		Vacuum cleaner		Washing machine	
	w_1	w_2	w_1	w_2	w_1	w_2	w_1	w_2	w_1	w_2	w_1	w_2
$Q_{0.25}$	5.67	2.90	7.52	4.98	3.46	8.78	7.35	7.59	8.14	4.35	9.37	0.20
$Q_{0.50}$	10.80	17.52	12.49	11.15	8.41	15.31	14.12	14.48	19.59	13.52	24.00	8.46
$Q_{0.75}$	25.23	30.62	34.57	18.60	18.83	30.81	28.30	34.01	38.67	24.14	62.52	23.53

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Table S5

Study 2—Probit Model: Estimated Parameter Ranges of the Attribute Weights (w_1 - w_2) and Variance (v)

Quantile	Digital camera			Color printer			Notebook computer			Racing bike			Vacuum cleaner			Washing machine		
	w_1	w_2	v	w_1	w_2	v	w_1	w_2	v	w_1	w_2	v	w_1	w_2	v	w_1	w_2	v
$Q_{0.25}$	0.33	0.04	0.00	0.37	0.20	0.00	0.00	0.58	0.00	0.27	0.24	0.00	0.19	0.11	0.00	0.41	0.05	0.00
$Q_{0.50}$	0.59	0.41	0.01	0.59	0.41	0.01	0.24	0.76	0.02	0.49	0.51	0.00	0.58	0.42	0.01	0.62	0.38	0.01
$Q_{0.75}$	0.96	0.67	0.08	0.80	0.63	0.21	0.42	1.00	0.40	0.76	0.73	0.04	0.89	0.81	0.19	0.95	0.59	0.69

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Table S6

Study 2—MDFT: Estimated Parameter Ranges of the Attribute Weights (w_1 - w_2), Variance (v), Decay Parameter (ϕ_2), Sensitivity

Parameter (ϕ_1), and Dominance Parameter wd

Quantile	Digital camera			Color printer			Notebook computer			Racing bike			Vacuum cleaner			Washing machine			ϕ_2	ϕ_1	wd
	w_1	w_2	v	w_1	w_2	v	w_1	w_2	v	w_1	w_2	v	w_1	w_2	v	w_1	w_2	v			
Q _{0.25}	0.30	0.05	0.01	0.46	0.26	0.01	0.12	0.48	0.02	0.33	0.36	0.03	0.39	0.27	0.03	0.53	0.06	0.01	0.05	28.68	1.09
Q _{0.50}	0.67	0.33	0.09	0.57	0.43	0.11	0.36	0.64	0.11	0.45	0.55	0.10	0.58	0.42	0.18	0.67	0.33	0.11	0.05	58.68	3.47
Q _{0.75}	0.95	0.70	1.16	0.74	0.54	0.47	0.52	0.88	3.30	0.64	0.67	1.84	0.73	0.61	0.51	0.94	0.47	0.56	0.06	93.20	11.85

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Table S7

Study 2—MDFT: Estimated Parameters of Selected Participants with $RST > .50$ and $PRST > .50$ Simultaneously for Attraction, Compromise, and Similarity Choice Triplets

Participant	Digital camera			Color printer			Notebook computer			Racing bike			Vacuum cleaner			Washing machine			ϕ_2	ϕ_1	wd
	w_1	w_2	v	w_1	w_2	v	w_1	w_2	v	w_1	w_2	v	w_1	w_2	v	w_1	w_2	v			
3	0.40	0.60	0.01	0.52	0.48	0.11	0.45	0.55	0.28	0.34	0.66	0.00	0.40	0.60	0.08	0.55	0.45	0.10	0.05	120.58	9.19
10	0.00	1.00	0.00	0.94	0.06	0.48	0.44	0.56	0.13	0.11	0.89	0.16	0.52	0.48	0.07	1.00	0.00	0.00	0.05	105.94	1.04
38	1.00	0.00	0.00	1.00	0.00	0.00	0.36	0.64	0.02	0.62	0.38	0.20	0.73	0.27	0.10	0.40	0.60	0.14	0.05	71.01	1.43

Reducing the MDFT to a Probit Model

This section shows how MDFT can be transformed into a probit model. Technically, this can be achieved by setting the feedback matrix and by omitting the variance–covariance matrix of the product-relevant attention weights.

One of the main differences between MDFT and a probit model is the dynamic aspect of MDFT. To reduce MDFT to a static model, such that the preference state \mathbf{P} remains constant over time, we set the feedback matrix \mathbf{S} to a zero matrix. A zero feedback matrix indicates no previous memory of previous preference states and no competition between the options (IIA property). Technically, a zero matrix for \mathbf{S} can be achieved by setting ϕ_2 to 1 (no memory of the previous preference state) and $\phi_1 \rightarrow \infty$.

In a next step, we set the variance–covariance matrix of the product-relevant attributes Ψ to zero, such that only the variance–covariance matrix of the product-irrelevant attributes remains. Ψ is calculated within the variance–covariance matrix of the valence vector \mathbf{V} . As described in Roe and colleagues (2001), the valence vector \mathbf{V} consists of the valence produced by product-relevant attributes $[\mathbf{C}\mathbf{M}_1\mathbf{W}_1(t)]$ and the valence of the product-irrelevant attributes $[\mathbf{C}\mathbf{M}_2\mathbf{W}_2(t) = \boldsymbol{\varepsilon}(t)]$ where \mathbf{C} is a contrast matrix to compute the momentary advantage or disadvantage of each option relative to the average of the other options. \mathbf{M}_1 represents a $J \times n$ subjective evaluation matrix, where J are the number of options and n are the number of attributes describing option j . $\mathbf{W}_1(t)$ is an $n \times 1$ vector containing the attention weights of each attribute i at time point t . The variance–covariance matrix of \mathbf{V} can be expressed as (Roe et al., 2001)

$$\begin{aligned} \text{Cov}[\mathbf{V}(t)] &= \text{Cov}[\mathbf{C}\mathbf{M}_1\mathbf{W}_1(t) + \boldsymbol{\varepsilon}(t)] = \mathbf{C}\mathbf{M}_1\text{Cov}[\mathbf{W}_1(t)]\mathbf{M}_1'\mathbf{C}' + \text{Cov}[\boldsymbol{\varepsilon}(t)] \\ &= \mathbf{C}\mathbf{M}_1\Psi\mathbf{M}_1'\mathbf{C}' + \varsigma = \Phi \end{aligned} \quad (\text{S1})$$

where

$$\Psi = \text{Cov}[\mathbf{W}_1(t)] = E[(\mathbf{W}_1(t) - \mathbf{w}_1)(\mathbf{W}_1(t) - \mathbf{w}_1)'] \quad (\text{S2})$$

is the variance–covariance matrix for the product-relevant weights and

$$\boldsymbol{\varsigma} = Cov[\boldsymbol{\varepsilon}(t)] = E[\boldsymbol{\varepsilon}(t)\boldsymbol{\varepsilon}(t)'] = \text{diag}(\boldsymbol{\varepsilon}(t)) \quad (\text{S3})$$

is the variance–covariance matrix of the product-irrelevant weights. If we assume that the attention shifts according to a Bernoulli process in an all-or-none manner from one attribute to another (see Appendix B of Roe et al., 2001), the probability of focusing on the product-relevant attributes can be written as

$$\mathbf{w}_1 = E[\mathbf{W}_1(t)]. \quad (\text{S4})$$

Accordingly, $\boldsymbol{\Psi}$ reduces to

$$\boldsymbol{\Psi} = \text{diag}(\mathbf{w}_1) - \mathbf{w}_1\mathbf{w}_1'. \quad (\text{S5})$$

By setting $\boldsymbol{\Psi}$ to a zero matrix, we reduce the variance–covariance matrix of \mathbf{V} to $\boldsymbol{\varsigma}$. To achieve this, we multiply $\boldsymbol{\Psi}$ by the scalar 0, which otherwise is set to 1. This turns

$\mathbf{CM}_1Cov[\mathbf{W}_1(t)]\mathbf{M}_1'C'$ into a zero matrix. Thus, only the covariance of the product-irrelevant attributes $\boldsymbol{\varsigma}$ remains. The assumption that the product-irrelevant attributes are uncorrelated with the product-relevant attributes and uncorrelated with each other implies that $Cov[\boldsymbol{\varepsilon}]$ is a diagonal matrix. Thus the variance–covariance matrix of the valence vector (\mathbf{V}) can be rewritten as

$$Cov[\mathbf{V}(t)] = Cov[\mathbf{V}] = Cov[\mathbf{CM}_1\mathbf{W}_1 + \boldsymbol{\varepsilon}] = 0 + Cov[\boldsymbol{\varepsilon}] = \text{diag}(\boldsymbol{\varepsilon}), \quad (\text{S6})$$

which is the same as the variance–covariance matrix of the (independent) probit model.